INTENSITY-BASED POINT-SPREAD-FUNCTION-AWARE REGISTRATION FOR MULTI-VIEW APPLICATIONS IN OPTICAL MICROSCOPY

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ABSTRACT
We present an algorithm to spatially register two volumetric datasets related via a rigid-body transform and degraded by an anisotropic point-spread-function (PSF). Registration is necessary, for example, when fusing data in multi-view microscopy. Automatic algorithms that only rely on maximizing pixel similarity, without accounting for the anisotropic image formation process, provide poor results in such applications. We propose to solve this problem by re-blurring the reference and test data with transformed forms of the PSF, in order to make them comparable, before minimizing the mean squared intensity difference between them. Our approach extends the pyramid-based sub-pixel registration algorithm proposed by Thévenaz et al., 1998, that employs an improved form of the Marquardt-Levenberg algorithm. We show, via simulations, that our method is more accurate than the conventional approach that does not account for the PSF. We demonstrate our algorithm in practice by registering multi-view volumes of a zebrafish larva acquired using a wide-field microscope.

Index Terms— Multi-view, registration, point-spread-function, Marquardt-Levenberg, pyramid, optical microscopy.

1. INTRODUCTION
Optical microscopy offers the unique possibility of imaging living samples under conditions akin to their native state. However, the technique often suffers from anisotropic resolution owing to the image formation process, which consists of a 3D convolution operation with the imaging system’s (anisotropic) point-spread-function (PSF) [1]. Despite recent advances to design instruments that exhibit nearly isotropic PSFs, many commonly used microscopes have a PSF that is more elongated in the axial direction, with wide-field microscopy having the most severe form of anisotropy, and techniques such as confocal, two-photon, and light-sheet microscopy having the least. This anisotropy translates to an axial resolution that is worse than the lateral resolution in the acquired data. Multi-view microscopy attempts to circumvent this problem by merging acquisitions from multiple tilted directions [1–7]. However, operations therein, such as multi-view fusion and deconvolution, require the volumes to be precisely registered before they can be used.

Several approaches have been proposed to address this registration problem. Heintzmann et al. [3] presented a mostly manual registration algorithm that relies on an interactive selection of salient points in the input volumes, which are used as an alignment aid. However, such a manual technique tends to be both laborious and inaccurate. A second class of algorithms that can be considered automatic relies on fiducial markers, such as fluorescent beads, added in moderate concentration to the prepared sample [8, 9], which are subsequently detected and used for registration. Although these approaches were shown to be accurate, they require a special method of sample preparation. Moreover, the markers added can interfere with the visibility of the sample being imaged. To alleviate this problem, Kricz et al. [6] designed an imaging system where such fiducial markers are only used for hardware calibration, thereby averting the need to add beads along with the sample during imaging. In lieu of external markers, Keller et al. [10] followed a data-specific strategy to automatically detect cell nuclei and treat them as landmarks for multi-view registration. Others have used techniques such as cross-correlation [1, 2, 4, 5] based on the pixel-wise similarity between datasets for registration. However, such approaches can lead to inaccuracies because they ignore the anisotropy inherent in the image formation process. A simple example is detailed in Fig. 1, where a sample (Fig. 1(a-c)) is convolved with an anisotropic PSF. The convolution shifts the optical center of mass (and other moments) in directions within the object coordinates [11] (Fig. 1(d-f)), leading conventional pixel-based matching methods (which would also match the center of mass) to yield a biased solution.

In this paper, we propose to modify the registration cost function by cross-blurring the reference and test datasets (Fig. 1(d-f)) using PSFs tilted by the candidate transformation, so that the image volumes are comparable and identically degraded at convergence (Fig. 1(g-i)). We demonstrate our approach using both simulations and experimental data.

The paper is organized as follows. In Section 2, we describe our notations, the cost function that we wish to minimize, and our optimization strategy. In Section 3, we illustrate the applicability of our method on simulated and experimental datasets, and finally conclude in Section 4.
Fig. 1: An illustration on how PSF affects data registration. The red circle denotes the center of mass in each case. (a-c) Registration of datasets uncorrupted by PSF. (d-f) Reference, test, and registered test, respectively. (g-i) Cross-blurred forms of the datasets in (d-f). Note that the center of mass coincides in (g) and (i), unlike that in (d) and (f).

2. METHOD

2.1. Problem Formulation

We consider a function $f(\mathbf{x})$, $\mathbf{x} \in \mathbb{R}^3$, that represents an object being imaged. We assume $f$ undergoes a geometric transformation that can be parameterized by (i) a rotation matrix, $\mathbf{A}$, of size $3 \times 3$, and (ii) a translation vector, $\mathbf{b}$, of size $3 \times 1$. We represent this using (i) a rotation operator, $R_\mathbf{A}$, and (ii) a translation operator, $T_\mathbf{b}$, defined as follows:

$$R_\mathbf{A} \{ f \} (\mathbf{x}) \triangleq f(A\mathbf{x})$$
$$T_\mathbf{b} \{ f \} (\mathbf{x}) \triangleq f(\mathbf{x} + \mathbf{b}).$$

We jointly express the parameters $\mathbf{A}$ and $\mathbf{b}$ as $\mathbf{p}$. We represent the sequence of transformations parameterized by $\mathbf{p}$ as:

$$Q_\mathbf{p} \{ f \} (\mathbf{x}) \triangleq (R_\mathbf{A} \circ T_\mathbf{b} \circ T_f) (\mathbf{x})$$
$$= f(A\mathbf{x} + \mathbf{b}),$$
$$Q_\mathbf{p}^{-1} \{ f \} (\mathbf{x}) \triangleq (T_{-\mathbf{b}} \circ R_{\mathbf{A}^{-1}} \circ T_f) (\mathbf{x})$$
$$= f(A^{-1}(\mathbf{x} - \mathbf{b})).$$

In particular, we consider two volumes—the reference $f_R$ and the test $f_T$ (which is to be geometrically transformed to match $f_R$) defined as follows:

$$f_R(\mathbf{x}) \triangleq (f * h)(\mathbf{x}),$$
$$f_T(\mathbf{x}) \triangleq (Q_\mathbf{p}^{-1} \{ f \} * h) (\mathbf{x}).$$

Specifically, $\mathbf{p}_*$ represents the unknown set of parameters ($\mathbf{A}_*$ and $\mathbf{b}_*$) that we wish to estimate and that characterize the geometrical transformation undergone by the object $f$ between the acquisitions of $f_R$ and $f_T$.

Fig. 2: The proposed cost function $\varepsilon^2$ to be minimized using cross-blurred forms of the reference $f_R$ and test $f_T$ datasets.

2.2. Proposed Registration Approach

The motivation of our approach stems from the fact that even if the correct geometrical transform $Q_{\mathbf{p}_*}$ is applied to the test data $f_T$, the resulting volume $Q_{\mathbf{p}_*} \{ f_T \}$ will be different from the reference $f_R$. This is because the geometrical transform $Q_{\mathbf{p}_*}$ also applies to the convolution kernel $h$, thus making an intensity-based similarity criterion unsuitable (Fig. 1(d-f)). To overcome this problem, we propose to cross-blur the reference and test data with each other’s effective PSF before using any candidate transform $Q_{\mathbf{p}}$ (Fig. 1(g-i)).

Using Eq. (7) in conjunction with properties of convolution operations, the convolution between $f_R$ and a rotated version of $h$ can be expressed as:

$$(f_R * R_\mathbf{A} \{ h \} ) (\mathbf{x}) = (f * h * R_\mathbf{A} \{ h \} ) (\mathbf{x}).$$

Similarly, using Eq. (8) and properties of affine transforms [12], applying $Q_{\mathbf{p}_*}$ after subjecting $f_T$ to a convolution with an inverse-rotated form of $h$ is equivalent to the following:

$$Q_{\mathbf{p}_*} \{ f_T * R_{\mathbf{A}_*^{-1}} \{ h \} \} (\mathbf{x}) = |\mathbf{A}_*| (Q_{\mathbf{p}_*} \{ f_T \} * h) (\mathbf{x})$$
$$= |\mathbf{A}_*|^2 (f * R_{\mathbf{A}_*} \{ h \} * h) (\mathbf{x}),$$

where $|\mathbf{A}|$ denotes the determinant of the matrix $\mathbf{A}$. For the correct transform, since the cross-blurred volumes are equivalent except for a scaling constant (compare Eqs. (9) and (11)), we can estimate the optimal set of parameters $\mathbf{p}_*$ via the following cost function (see also Fig. 2):

$$\varepsilon^2(\tilde{\mathbf{p}}) \triangleq \left\| A \{ f_R * R_\mathbf{A} \{ h \} \} (\mathbf{x}) - \left\| A \{ f_T * R_\mathbf{A} \{ h \} \} (\mathbf{x}) - (Q_{\mathbf{p}_*} \{ f_T \} * h) (\mathbf{x}) \right\|^2_2$$

$$= \left\| A \{ f_R * R_\mathbf{A} \{ h \} \} (\mathbf{x}) - (Q_{\mathbf{p}_*} \{ f_T \} * h) (\mathbf{x}) \right\|^2_2$$

where $\tilde{\mathbf{p}}$ comprises $\mathbf{A}$ and $\mathbf{b}$. Since $|\mathbf{A}| = 1$ when $\mathbf{A}$ is a rotation matrix, we can ignore this scaling constant for all purposes in this paper.

To estimate the optimal set of parameters $\mathbf{p}_*$, we solve a variant of $\partial \varepsilon^2(\tilde{\mathbf{p}})/\partial \tilde{\mathbf{p}} = 0$ with an improved form of the
3. EXPERIMENTS

3.1. Validation with simulated data

For validation purposes, we considered a synthetic dataset consisting of six parallel hollow bars [15] (Fig. 3(a-b)) as our uncorrupted volume, \( f \). We then used a software package [16] to generate a Gibson & Lanni 3D PSF model (Fig. 3(c)), \( h \), applicable for wide-field microscopes, with the following parameters: immersion refractive index = 1 (air), sample refractive index = 1.33, numerical aperture (NA) = 0.7, working distance = 2 mm, particle position = 0 \( \mu \text{m} \), sampling step \( \Delta x = \Delta y = \Delta z = 0.5 \mu \text{m} \), excitation wavelength = 495 nm, and emission wavelength = 509 nm. Using \( f \) and \( h \), we generated the reference \( f_R \) (Fig. 3(d)). Next, we rotated \( f \) by an angle of 30° about the \( x \)-axis, and translated it by a vector \([b_0, b_1, b_2]^\top\) where \( b_0, b_1, \) and \( b_2 \) were chosen from a uniform distribution between 0 and 5, and finally convoluted it with \( h \) to form \( f_T \) (Fig. 3(e)). With an initial guess equal to the identity transformation, we then attempted to estimate \( p_s \) using two different approaches: (i) using the PSF ignorant form of the improved ML algorithm [14] (i.e., assuming \( h(\mathbf{x}) = \delta(\mathbf{x}) \)), and (ii) using our proposed algorithm. The simulation was run over 10 random instances, and the mean error in the estimated angle was found to be 11.55° using the traditional approach, and 1.71° using our proposed algorithm. Examples of the registered results obtained using the two algorithms are shown in Fig. 3(f) and (g), respectively. We repeated this experiment by also using a Gaussian approximation of the PSF corresponding to a disk scanning confocal microscope [17] with NA = 0.3, pinhole radius = 5 Airy units, and similar parameters as before. For this case, the mean error in the estimated angle was recorded as 5.69° using the traditional approach, and 0.39° using our proposed algorithm.

3.2. Illustration on experimentally acquired data

To prove the applicability of our approach for experimental datasets, we used an inverted wide-field microscope equipped with a 10×/0.3 dry objective to acquire 3D volumes of a 25-hpf (hours post-fertilization)-old transgenic zebrafish larva (\( \text{Tg(fli1a:EGFP)} \)), which expresses green fluorescent protein in the vasculature. We inserted the larva in a tube made from fluorinated ethylene propylene (FEP), whose refractive index is close to that of water, and rotated the tube using a stepper motor for six multi-view acquisitions (Fig. 4(d)). Treating the first volume as the reference, we recursively registered each subsequent dataset to its aligned predecessor. The registered form of the final volume is shown together with the first reference in Fig. 4(a-c). The results demonstrate that despite the anisotropic resolution, characteristic of wide-field microscopy, our approach correctly matches the curvature and bright features of the vasculature, without erroneously matching the dominant blur (see also supplemental movie).

4. CONCLUSION

We have derived an automatic intensity-based registration routine and have demonstrated its suitability for aligning volumes that were acquired using imaging systems with severely anisotropic point spread functions. The simulation results, which showed an accuracy of around an order of magnitude over the traditional scheme, demonstrates the benefits of such an approach that integrates the imaging model. The good alignment we observed using multi-view volumes from a
Fig. 4: (a-c) MIP of the first volume (green) and the recursively registered final volume (magenta) (originally acquired after a rotation of approximately 90° about the x-axis) in the xy, yz, and xz planes, respectively. (d) A schematic representation showing the relative position of the sample and the axis of rotation in our experimental setup. Scale bar is 200µm.

wide-field microscope, whose PSF anisotropy is particularly strong, confirms our method’s potential for applications in multi-view microscopy.

5. REFERENCES


