

# Weighted Correlation based Atom Decomposition Intonation Modelling

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## Abstract

Intonation modelling is an integral part of text-to-speech systems from their very beginnings. This has led to the proliferation of various intonation models, each with its own relative strengths and weaknesses. Only a few of these intonation models are based on physiology, despite the advantage that such models are language independent. We propose a new intonation model inspired by the physiology of intonation production, which is based on decomposing the  $F_0$  contour into elementary atoms. The model, named the Weighted Correlation Atom Decomposition model (WCAD), is a generalisation of the command response (CR) model and has the advantage of having a simple parameter extraction method. The decomposition process follows a matching pursuit approach based on using the perceptually relevant weighted correlation as a cost function. The results have affirmed the plausibility of using the WCAD model to model  $F_0$  contours across different languages and speakers. The results have also shown that the WCAD model has good comparative performance to the CR model, giving it practical importance.

**Index Terms:** intonation model, physiology, matching pursuit, weighted correlation

## 1. Introduction

Current state of the art text-to-speech (TTS) synthesis systems are able to produce speech with reasonably good quality. However, one issue in TTS is the still unsatisfactory prosody of the synthetic speech. As an important part of prosody, intonation is one of the research areas that remain open in TTS. Many different approaches to intonation modelling can be found in the literature, but only a few of them are trying to model the production of intonation [1, 2, 3].

The command-response (CR) model [1] is the most popular in this category and more generally one of the most popular intonation models. It defines intonation by looking at the physiological process behind its production. Relating the vocal folds' tension with the activity of the muscles ruling them, Fujisaki showed that the fundamental frequency can be decomposed in several additive components in the log domain [4]. In this model, two different types of components are credited to the translation and rotation of the cricothyroid (CT) muscle.

Strik [5] identified more muscles at work in the production of  $F_0$ , as well as the influence of the subglottal pressure  $P_{sb}$ . In our previous work, we investigated a generalisation of the CR model that would account for more than 2 types of movements influencing the  $F_0$  production [6]. Following some work on modelling intonation using the CR model [7, 8], we replaced the step functions used for local components in the CR model

by impulses. By defining all the components of the model as impulse responses to a critically damped system, we argue that these components could be linked to the response of the muscles involved in intonation generation. The parameters of this model also present the advantage of being easy to extract using the matching pursuit algorithm [9], followed by a selection of the relevant atoms using a weighted root mean square distance.

In this paper, we present further development of our model by directly extracting relevant atoms by using weighted correlation; the perceptual relevance of the weighted correlation is discussed. We also present a different definition for the global component of intonation. The paper is structured as follows: Section 2 presents the weighted correlation-based decomposition method, Section 3 describes the experiments, Sections 4 and 5 give results and conclude the paper.

## 2. Weighted Correlation based Atom Decomposition

The Weighted Correlation based Atom Decomposition (WCAD) algorithm is based on the integration of the modified version of the perceptually relevant weighted correlation (WCORR) measure [10] as a cost function in the matching pursuit framework [9]. The algorithm is an improved and more compact version of the algorithm we presented in our previous work [6], which was based on using the weighted RMS error (WRMSE) to filter out the perceptually irrelevant atoms output by the matching pursuit algorithm. The WCAD algorithm also introduces a novel physiologically inspired type of atom for representing the global, i.e. phrase component in the  $F_0$  contour.

### 2.1. Weighted Correlation

The weighted RMS and the weighted correlation measures were both first introduced in the work of Hermes [10]. In his work, Hermes found that the WCORR measure had the best correlation (0.67) with the auditory dissimilarity ratings of five experienced phoneticians. This is a solid correlation, having in mind that the interexpert agreement was found to be 0.65, in the same work. Moreover, Hermes found approximate thresholds that can be used to classify the perceptual similarity of two intonation contours using the WCORR, given in Table 1.

The weighted correlation (WCORR) introduced by Hermes [10] is calculated according to (1). Here  $f_0$  is the reference  $F_0$ ,  $\hat{f}_0$  is the modelled  $F_0$ , i.e. its reconstruction,  $f_{0m}$  and  $\hat{f}_{0m}$  are their respective means, and  $w(i)$  is the weighting function. Originally, the weighting function was defined as the maximum amplitude of the subharmonic sumspectrum (SHS), which is a

weighted sum of the harmonics contributing to the pitch [11].

$$r = \frac{\sum_i w(i)(\hat{f}_0(i) - \hat{f}_{0m})(f_0(i) - f_{0m})}{\sqrt{\sum_i (w(i)(\hat{f}_0(i) - \hat{f}_{0m})) \sum_i (w(i)(f_0(i) - f_{0m}))}} \quad (1)$$

In our WCAD algorithm, we use a modified version of the WCORR, given in 2, in which we alter the originally proposed WCORR in three ways. 1) We do not subtract the mean of the  $F_0$  contours, as our model does not have a static component, and we need the extracted atoms to build up the  $F_0$  contour from scratch. 2) We use the logarithm of the  $F_0$ , instead of the equivalent rectangular bandwidth (ERB) scale [12], because it is both traditionally used in intonation modelling research [1], and is also essentially equivalent to the use of semitones in perceptual intonation studies [13, 14]. 3) We redefine the weight according to (3), abandoning the deprecated SHS spectrum, and in accordance with newer trends in perceptual intonation studies [14, 13]. Here,  $p(i)$  is the probability of voicing (POV) of frame  $i$  as defined by Ghahremani et al. [15], and  $e(i)$  its energy. The use of a continuous POV estimate, instead of using a binary thresholded one [13], eliminates the use of hard thresholds, making the weighting function more robust.

$$r = \frac{\sum_i w(i)\hat{f}_0(i)f_0(i)}{\sqrt{\sum_i w(i)\hat{f}_0(i)\sum_i w(i)f_0(i)}} \quad (2)$$

$$w(i) = p(i)e(i) \quad (3)$$

## 2.2. Phrase atoms

In our previous work [6], we introduced the use of general gamma form atoms, defined according to (4), as the building blocks of the  $F_0$  contour. This is based on a higher-order extension of the critically-damped second-order linear systems [16] that account for the phrase and accent commands in the original command-response model [1].

$$G_{k,\theta}(t) = \frac{1}{\theta^k \Gamma(k)} t^{k-1} e^{-t/\theta} \quad \text{for } t \geq 0 \quad (4)$$

The problem with the use of gamma distribution shaped function to model the phrase atom is that the high  $\theta$ -s needed to produce atoms with a sufficiently gradual fall, also stretched out the rise of the atoms and their peaks. This is in contrast to the qualitative shape of the global component of the subglottal pressure  $P_{sb}$ , as seen in the measurements of Strik [5]. There, the global component has a steeper rise with a relatively sharp peak at the start of phonation, which is followed by a lengthy fall. This reflects the initial buildup of  $P_{sb}$  that precedes speech, and its timely release for the purpose of sustaining phonation. We seek to capture this observed quality of the global  $P_{sb}$  component using a modified definition of the phrase atom, based on

Table 1: Weighted correlation thresholds for five perceptual similarity categories of two  $F_0$  contours found by Hermes [10].

Category	WCORR	Perceptual $F_0$ similarity
1	$> 0.978$	no differences
2	$> 0.946$	differences audible
3	$> 0.896$	differences clearly audible
4	$> 0.827$	linguistic differences
5	$< 0.827$	completely different

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## Algorithm 1 Weighted Correlation Atom Decomposition algorithm.

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1: procedure WCORR ATOM DECOMPOSITION
2:   Extract  $f_0$ ,  $e$  and  $p$  from waveform.
3:   Calculate  $w$  from  $e$  and  $p$ .
4:   Extract  $t_s$  and  $t_e$  of phonation.
5:   Find  $\theta_f$  for phrase atom at position  $t_s$  giving max
   WCORR for  $t_s \leq t \leq t_e - t_{off}$ .
6:   Calculate phrase atom amplitude using correlation.
7:    $f_{diff} = f_0 - \text{phrase atom}$ .
8:    $f_{recon} = \text{phrase atom}$ .
9:   Loop:
10:  Extract local atom giving max WCORR with  $f_{diff}$  for
    $t > t_s$ .
11:  Calculate local atom amplitude using correlation.
12:  Increment atom count.
13:   $f_{diff} = f_{diff} - \text{local atom}$ .
14:   $f_{recon} = f_{recon} + \text{local atom}$ .
15:  if  $\text{WCORR}_{\text{norm}} \text{ of } f_{recon} > \text{WCORR}_{\text{norm}} \text{ thresh}$  then
16:    goto End.
17:  else
18:    goto Loop.
19: End.

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the concatenation of two gamma distribution functions:

$$G_{k,\theta_r,\theta_f}(t) = \begin{cases} \frac{1}{\theta_r^k \Gamma(k)} t^{k-1} e^{-t/\theta_r} & \text{for } 0 \leq t \leq t_m \\ \frac{1}{\theta_f^k \Gamma(k)} (t - t_o)^{k-1} e^{-(t-t_o)/\theta_f} & \text{for } t > t_m \end{cases} \quad (5)$$

Here,  $\theta_r$  and  $\theta_f$  are the two time constants for the rise and fall of the phrase atom,  $t_m$  is the time instant of the phrase atom peak, and  $t_o$  is an offset meant to compensate for the difference between  $t_m$  and the maximum of the fall function  $t_{fm}$ :

$$t_o = t_m - t_{fm}. \quad (6)$$

## 2.3. WCAD model extraction

The Weighted Correlation Atom Decomposition (WCAD) algorithm is outlined in Algorithm 1. First, the algorithm extracts the energy  $e$ ,  $f_0$  and POV  $p$ , and calculates the weighting function  $w$ . Next, the start and end times of phonation,  $t_s$  and  $t_e$ , are estimated by finding the time instants when the energy  $e$  crosses a start threshold value  $T_s$ , and when it finally goes below a terminal threshold value  $T_e$ . The phrase atom peak is then positioned at  $t_s$ , and we find the  $\theta_f$  that maximizes the WCORR (2) within a range between  $t_s$  and  $t_e - t_{off}$ . Here,  $t_{off}$  is an offset time introduced to leave out a possible phrase-final fall and rise in the  $F_0$  contour from the phrase atom fitting. Also, we use a fixed value for  $\theta_r$  due to the consistency in rise times across the utterances observed in Strik's measurements [5]. The amplitude of the phrase atom is calculated using the standard correlation, and is subtracted from  $f_0$  to obtain  $f_{diff}$ . The phrase atom is also used to initialise the  $F_0$  reconstruction  $f_{recon}$ .

In the second part of the atom decomposition, local atoms are extracted from  $f_{diff}$  using the WCORR, by selecting the atom that maximises it at each iteration. The amplitude of the extracted atoms is again calculated using the standard correlation, and they are subtracted from  $f_{diff}$ , and added to  $f_{recon}$ . Local atom extraction ends when either a) the reconstruction  $f_{recon}$  reaches a selected  $\text{WCORR}_{\text{norm}}$  threshold, or b) when the chosen maximum number of atoms is reached. Here,

WCORR<sub>norm</sub> includes the zero-mean normalisation of the two  $F_0$  contours as in (1), which allows us to use the WCORR perceptual thresholds from Table 1 as a stopping criterion. We argue that this is plausible, because the weight used by the WCAD algorithm essentially captures the same information as the originally proposed SHS. A formal proof of this is beyond the scope of the paper.

### 3. Experiments

We have designed two experiments to assess the plausibility of the introduced Weighted Correlation Atom Decomposition algorithm, and to compare its performance with a state of the art implementation of the standard CR model, as it is a generalised CR model.

**Experiment 1.** Our first goal is to analyse how well the WCAD algorithm models the  $F_0$  contour. To assess this, we will analyse how much the addition of each local atom increases the WCORR<sub>norm</sub> between the original and modelled  $F_0$  contours. We expect the WCORR to increase rapidly as the initial large local atoms are added and saturate at the optimal number of atoms per syllable. We also evaluate the number of atoms per syllable necessary to match the perceptual WCORR thresholds from Table 1. To extract the  $F_0$  and the POV we will use the pitch tracker implemented in Kaldi [15]. It generates a continuous  $F_0$  contour through the use of interpolation and smoothing.

**Experiment 2.** In order to compare the performance of the WCAD algorithm with the CR model, we use Mixdorff's CR parameter extraction tool [17]. Because this tool only outputs the final optimised CR model parameters, the calculated WCORR<sub>norm</sub> for the modelled  $F_0$  will be plotted as single points in the WCORR – atoms/syl plain, and then compared to the results obtained with the WCAD algorithm. The average WCORR and number of commands per syllable, obtained with the CR model per speaker, will also be used in the comparison.

#### 3.1. Database

The experiments were run on the same dataset used in our previous work [6]. This dataset contains a total of 60 utterances, and comprises recordings of 6 different speakers and 3 different languages: English, French and German. For each language, a male (M) and a female (F) speaker were chosen: *rjs* (M), released for Blizzard Challenge 2010<sup>1</sup> and *slt* (F) for English [18], *Bernard* (M)<sup>2</sup> and *Isabelle Brasme* (F)<sup>3</sup> for French and *spid* (M) and *alzn* (F) for German [19].

#### 3.2. WCAD algorithm parameters

The parameters used in the WCAD algorithm were determined through qualitative assessment of its performance on a set of randomly chosen utterances. It's reasonable to suppose that these are speaker dependent, but for the purpose of this paper we pull them together and assume speaker independence.

To determine the start of phonation  $t_s$ , we chose a threshold value  $T_s$  for the normalised energy of 0.5. For the end of phonation  $t_e$ , the threshold  $T_e$  was lowered to 0.1, because of the gradual decrease of energy towards the end of an utterance. The offset time  $t_{off}$  subtracted from  $t_e$  to leave out possible phrase-final falls and rises in  $F_0$  was set to 150 ms.

<sup>1</sup>[http://www.synsig.org/index.php/Blizzard\\_Challenge\\_2010](http://www.synsig.org/index.php/Blizzard_Challenge_2010)

<sup>2</sup><https://librivox.org/a-lombre-des-jeunes-filles-en-fleur-by-marcel-proust-0905/>

<sup>3</sup><https://librivox.org/la-princesse-de-cleves-by-madame-de-la-fayette/>

Table 2: Number of atoms/syllable needed on average to reach a chosen perceptual similarity category, for each of the speakers.

Cat.	en M	en F	fr M	fr F	ge M	ge F	Avg.
1	0.71	0.79	0.38	0.49	0.75	0.83	0.66
2	0.48	0.42	0.29	0.30	0.47	0.53	0.41
3	0.34	0.27	0.19	0.19	0.32	0.39	0.28
4	0.26	0.17	0.14	0.12	0.24	0.24	0.19

The  $\theta_r$  for the rising part of the phrase atoms was fixed at 0.5. The range for the  $\theta_f$  of the phrase atoms was set to 0.1 - 10, and for the  $\theta$  of the local atoms to 0.01 - 0.05. These two ranges give the needed atom variability in the WCAD algorithm. The values  $k$  in the atom gamma distribution shaped function 4 was set to 6, as it was found to have a slightly better overall performance than the  $k$  of 4 used in our previous work [6].

### 4. Results

Example results of the Weighted Correlation based Atom Decomposition algorithm are given in Fig. 1 for an utterance taken from the male French speaker in our database. The top panel shows the original  $F_0$  contour, the extracted phrase atom and the reconstructed  $F_0$  by our model. The local atoms that compose this contour are given in the middle panel. Finally, the bottom panel shows the energy contour, the POV, and the calculated weight, all normalised to 1. Only the larger local atoms were used in this reconstruction for clarity.

We can see that the WCAD algorithm successfully decomposes the  $F_0$  contour. The phrase component gives a qualitatively good fit to the global trend of the  $F_0$ , and the phrase-final drop is successfully captured. Also, the algorithm uses both positive and negative atoms to decompose the  $F_0$  contour, which is in line with Strik's findings [5], and increases its physiological plausibility.

**Experiment 1.** The results of the first experiment are presented in Fig. 2 for the English male speaker. The figure shows plots of the WCORR<sub>norm</sub> relative to the number of atoms per syllable for the 10 utterances recorded by this speaker, and the average curve that is representative of how well the WCAD algorithm models this particular speaker. As expected, the WCORR curves rise steeply at the beginning as the larger local atoms are added, and eventually saturate as smaller and smaller atoms are added. It is interesting to note that saturation is reached around the 1 atom/syllable mark, which might hint at a deeper physiological plausibility of our model. Average WCORR<sub>norm</sub> plots were calculated for all of the speakers and are shown in Fig. 3. We can see that the average curves vary across the different speakers and languages, but that they also correlate well and follow the same general trend.

Table 2 gives the number of atoms per syllable needed on average for the WCAD algorithm to model the  $F_0$  curve to the different perceptual WCORR thresholds presented in Table 1, for each of the speakers. Again we can see that there is a variability among the speakers, but there seems to be some correlation within the languages themselves, which is a matter for further investigation. The average atoms/syl is also given for each category.

**Experiment 2.** To compare the performance of our algorithm with that of the CR model, we plotted the results obtained with Mixdorff's CR parameter extraction in Fig. 3 with single points for each utterance for each of the speakers. We can see that our algorithm seems to give comparatively good results to the CR model, asserting its practical value. Note that for some

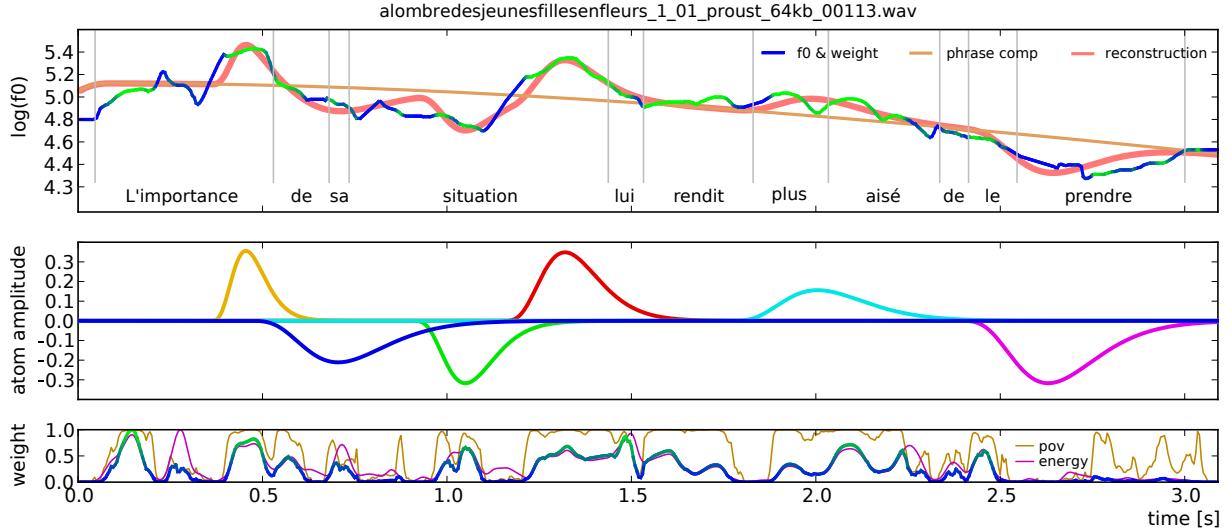


Figure 1: Results obtained with the WCAD algorithm for the sentence “L’importance de sa situation lui rendit plus aisé de le prendre.” by the French male speaker, showing the: original  $F_0$ , colored according to POV, phrase atom and reconstructed  $F_0$  (top), extracted local atoms (middle), and the energy, the POV and the weighting function (bottom).

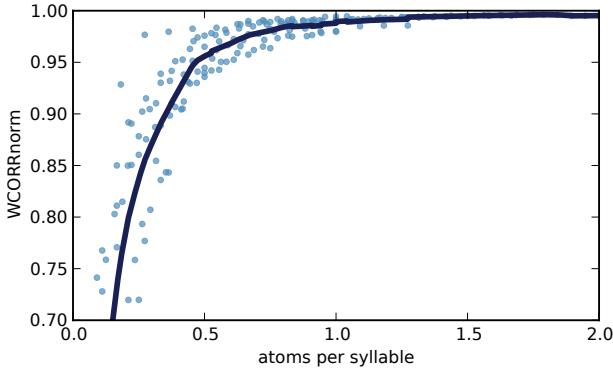


Figure 2: Weighted correlation of the WCAD algorithm  $F_0$  contours relative to the number of atoms per syllable for all of the sentences for the English male speaker, and the calculated average curve.

Table 3: Average WCORR and number of atoms/syllable obtained by the CR model, for each of the speakers.

	En M	En F	Fr M	Fr F	Ge M	Ge F	Avg.
WCORR	0.973	0.964	0.967	0.976	0.967	0.969	0.969
Cat	2	2	2	2	2	2	2
commands	17	12	24	22	14	10	16
com/syl	0.46	0.42	0.37	0.37	0.42	0.47	0.42

of the utterances the extraction of the CR model parameters with Mixdorff’s implementation failed and they are not included in the plot.

Table 3 gives the average WCORR and the average total number of phrase and accent commands in the CR model for each of the speakers. The results show that Mixdorff’s implementation of the CR model on average gives a WCORR of 0.97, which corresponds to Category 2 from Table 1, at 0.42 atoms/syl. When comparing the average number of atoms/syl with those obtained with the WCAD algorithm, we can see that our algorithm obtains the same perceptual quality with nearly the same average number of atoms/syl.

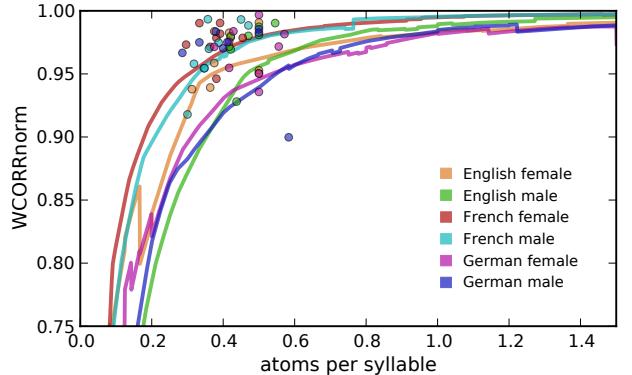


Figure 3: Weighted correlation of the  $F_0$  contours relative to the number of atoms per syllable averaged over all the sentences for each of the speakers in the database. The WCORRs obtained with Mixdorff’s implementation of the CR model are shown for comparison.

## 5. Conclusions

We have introduced a generalised CR model called the Weighted Correlation Atom Decomposition model. The model was designed to qualitatively approximate the physiological processes of intonation production. The atom decomposition process is fully automatic and is based on a matching pursuit framework, which integrates the perceptually relevant weighted correlation as a cost function. The introduced model has been shown to successfully model the intonation contours across a number of speakers and languages affirming its plausibility. In addition, it has been shown that the introduced model has comparable performance to the CR model, proving its practical value to modelling intonation in text-to-speech.

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